

MATH 530, REAL ANALYSIS, SPRING 2017

The course will cover most of the sections in this list.

1. ABSTRACT INTEGRATION

- (1) Set-theoretic notations and terminology (read ahead)
- (2) The concept of measurability
- (3) Simple functions
- (4) Elementary properties of measures
- (5) Arithmetic in $[0, \infty]$
- (6) Integration of positive functions
- (7) Integration of complex functions
- (8) The role played by sets of measure zero

2. POSITIVE BOREL MEASURES

- (1) Vector spaces
- (2) Topological preliminaries
- (3) The Riesz representation theorem
- (4) Regularity properties of Borel measures
- (5) Lebesgue measure
- (6) Continuity properties of measurable functions

3. L^p -SPACES

- (1) Convex functions and inequalities
- (2) The L^p -spaces
- (3) Approximation by continuous functions

4. ELEMENTARY HILBERT SPACE THEORY

- (1) Inner products and linear functionals
- (2) Orthonormal sets
- (3) Trigonometric series

5. EXAMPLES OF BANACH SPACE TECHNIQUES

- (1) Banach spaces
- (2) Consequences of Baire's theorem
- (3) Fourier series of continuous functions
- (4) Fourier coefficients of L^1 -functions
- (5) The Hahn-Banach theorem
- (6) An abstract approach to the Poisson integral

6. COMPLEX MEASURES

- (1) Total variation
- (2) Absolute continuity
- (3) Consequences of the Radon-Nikodym theorem
- (4) Bounded linear functionals on L^p
- (5) The Riesz representation theorem

8. INTEGRATION ON PRODUCT SPACES

- (1) Measurability on cartesian products
- (2) Product measures
- (3) The Fubini theorem
- (4) Completion of product measures
- (5) Convolutions
- (6) Distribution functions

18. ELEMENTARY THEORY OF BANACH ALGEBRAS

- (1) Vector spaces
- (2) Topological preliminaries
- (3) The Riesz representation theorem
- (4) Regularity properties of Borel measures
- (5) Lebesgue measure
- (6) Continuity properties of measurable functions